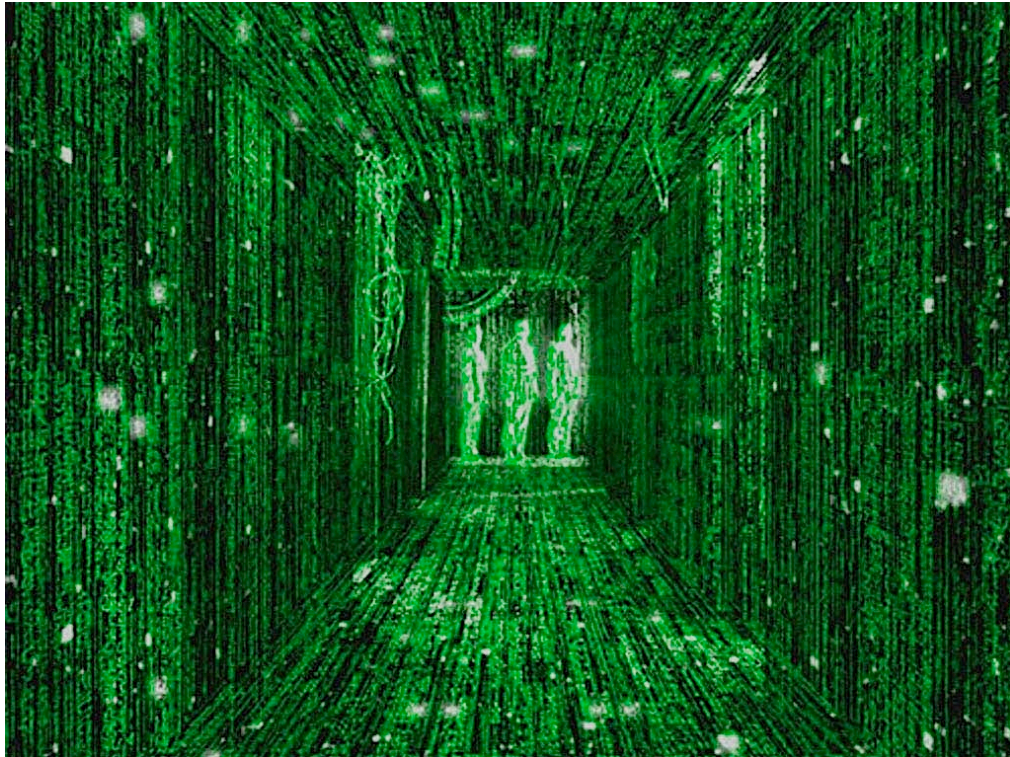


# *Exclusive Diffractive Vector Meson Production in eA: Finding the Source*



*Thomas Ullrich  
October 4, 2012*

# *Exclusive Diffractive Vector Meson Production in eA: Finding the Source Distribution*



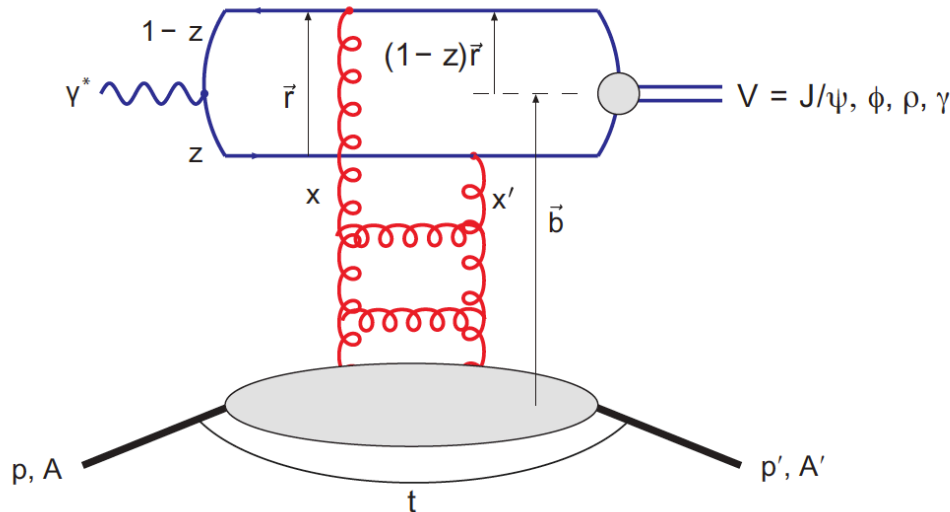
*Thomas Ullrich  
October 4, 2012*

# Reminder

$e + A \rightarrow e' + A + V$  where  $V = J/\psi, \phi, \rho, \gamma$

- Amplitude for producing an exclusive vector meson or a real photon diffractively is:

$$\begin{aligned} \mathcal{A}_{T,L}^{\gamma^* p \rightarrow V p}(x, Q, \Delta) = & i \int dr \int \frac{dz}{4\pi} \int d^2\mathbf{b} (\Psi_V^* \Psi)(r, z) \\ & \cdot 2\pi r J_0([1-z]r\Delta) \\ & \cdot e^{-i\mathbf{b} \cdot \Delta} \frac{d\sigma_{q\bar{q}}^{(p)}}{d^2\mathbf{b}}(x, r, \mathbf{b}) \end{aligned}$$



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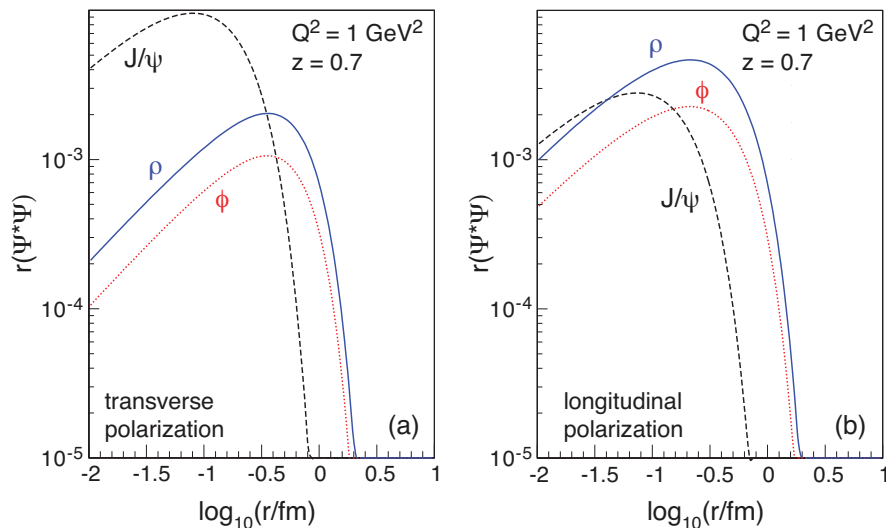
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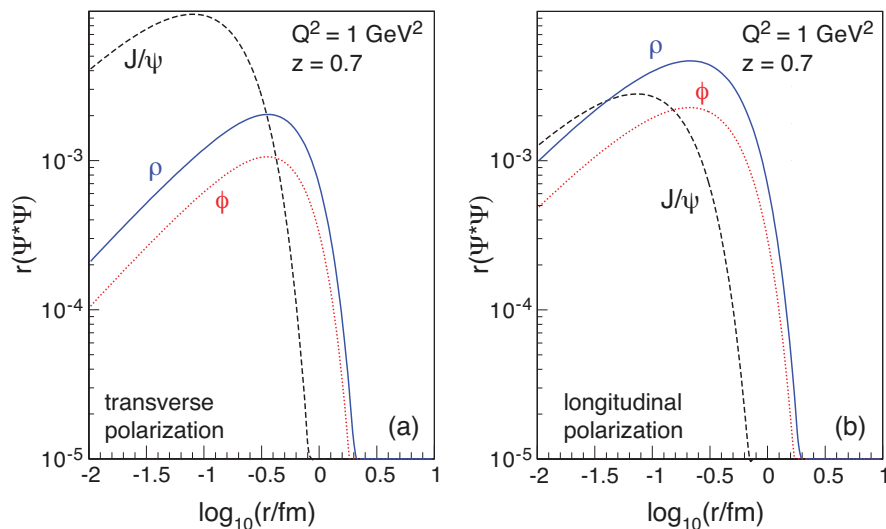


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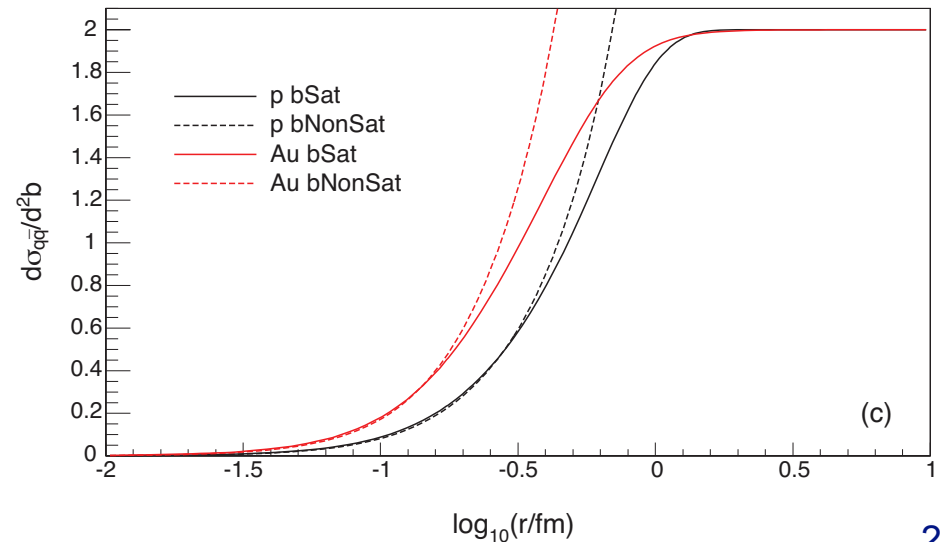
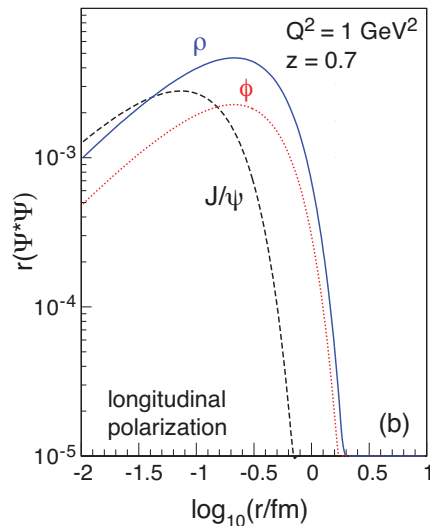
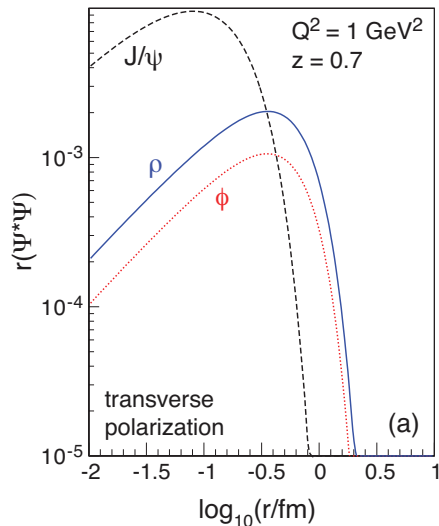


# Reminder

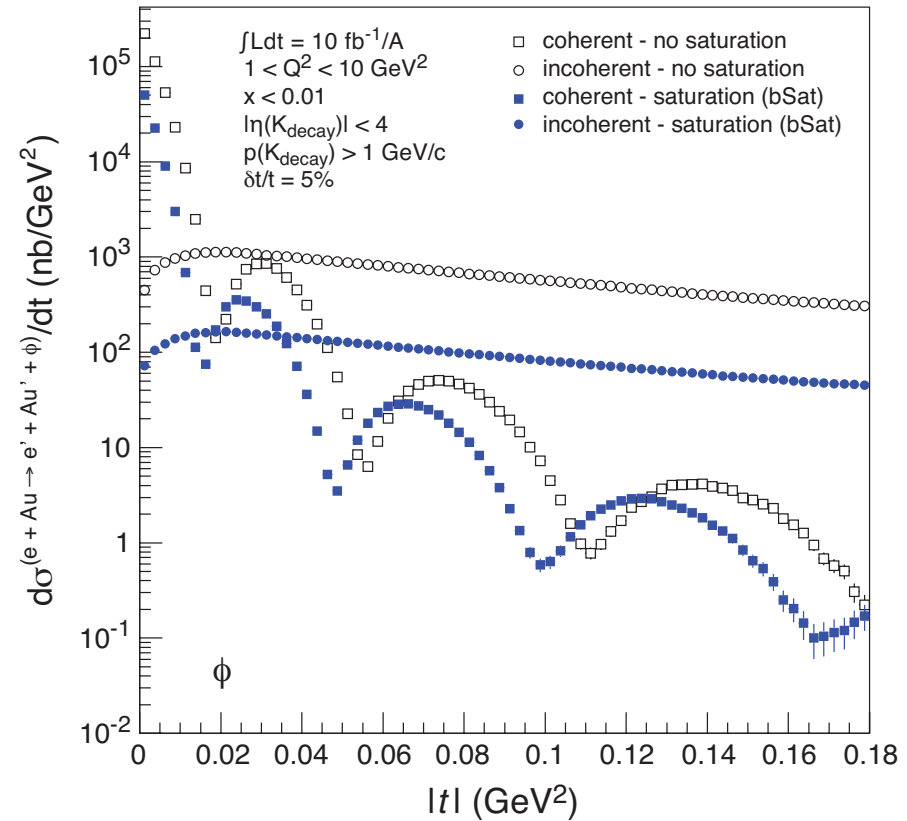
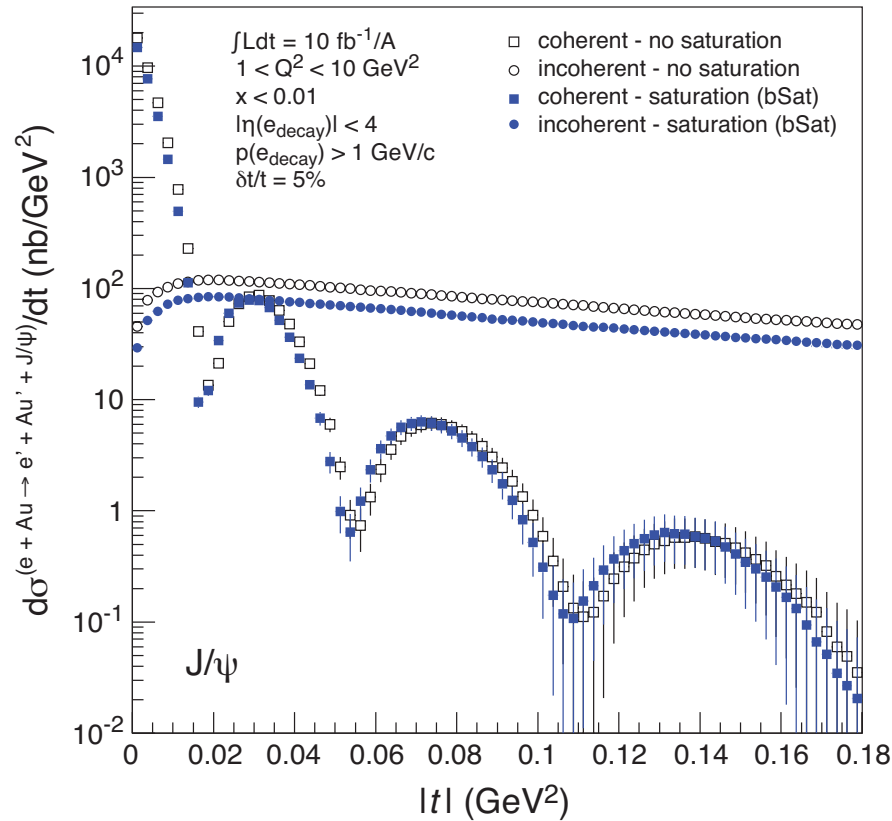
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# Starting Point



## Reminder:

- $e + Au \rightarrow e' + Au + J/\psi$ : not sensitive to sat. effects
- $e + Au \rightarrow e' + Au + \phi$ : larger wf  $\Rightarrow$  sensitive to sat. effects
- Sartre: uses Woods-Saxon to generate nuclei



# Getting Source Distribution from $d\sigma/dt$

Markus Diehl (INT '10):

$$F(b) \sim \frac{1}{2\pi} \int_0^{\infty} d\Delta \Delta J_0(\Delta b) \sqrt{\frac{d\sigma}{dt}}$$

$$t = \Delta^2/(1-x) \approx \Delta^2 \quad (\text{for small } x)$$

Issues (ep):

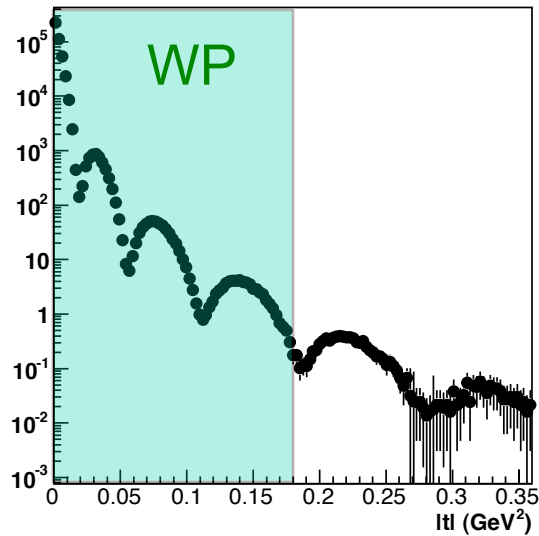
- Measured range in  $\Delta$
- Statistical errors on data

What about eA?

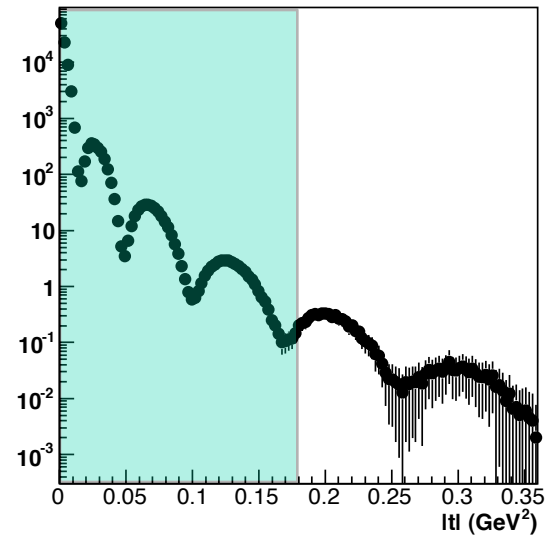
- WP: only shows  $d\sigma/dt$  for  $t < 0.16 \text{ GeV}^2$
- Available simulations extend to  $t = 0.36 \text{ GeV}^2$
- Is this enough to extract a reasonable  $F(b)$ ?
- Are errors even at  $10 \text{ fb}^{-1}$  a killer?

# Available Data from Sartre (100M each)

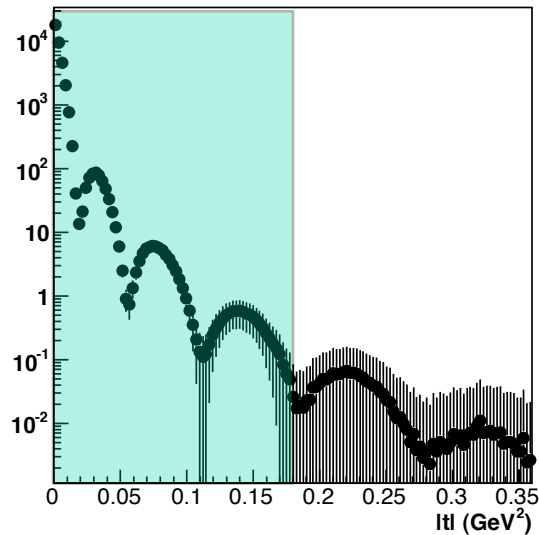
phi nosat



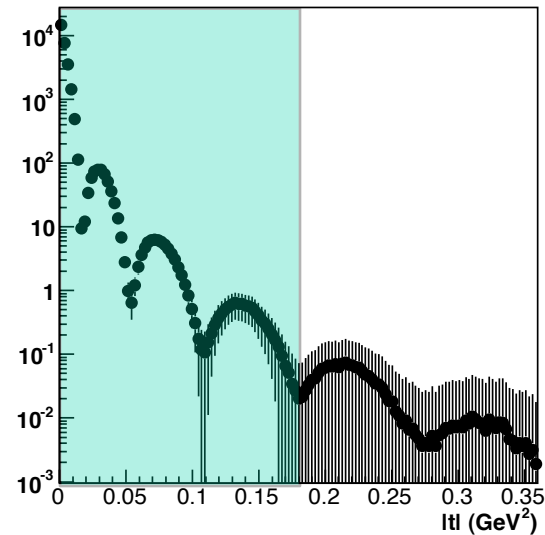
phi sat



jpsi nosat



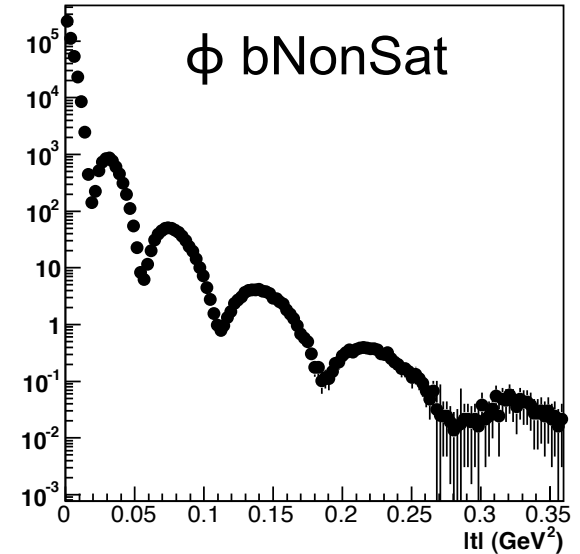
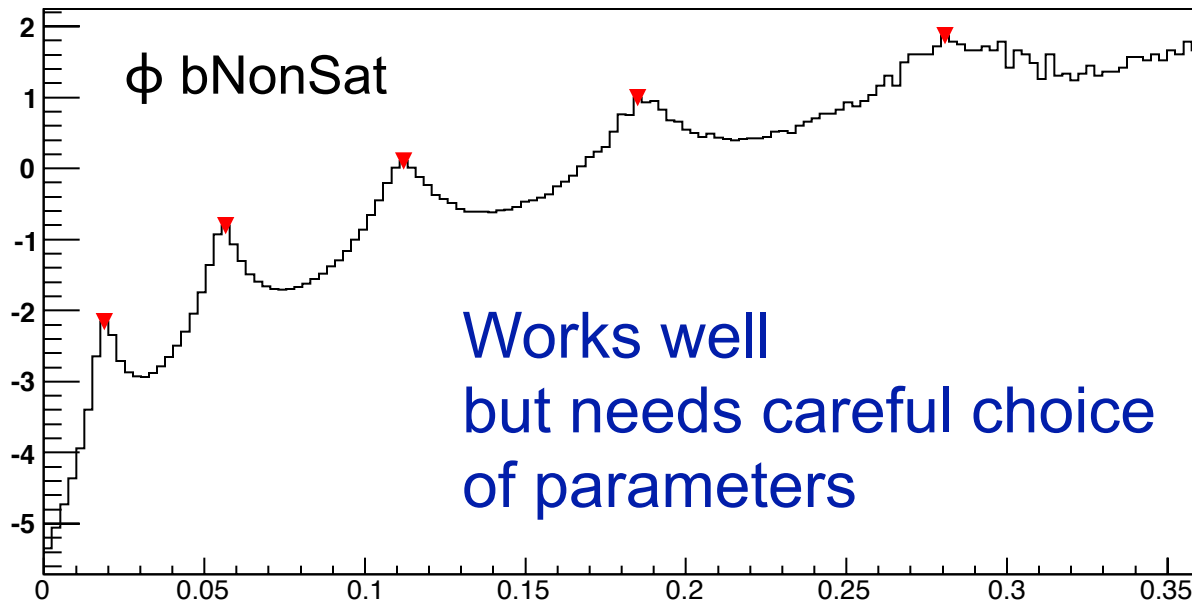
jpsi sat



# Practical Issues

For integration: Sign flip in  $J_0(\Delta b)$ ?

Use ROOT::TSpectrum::Search package:

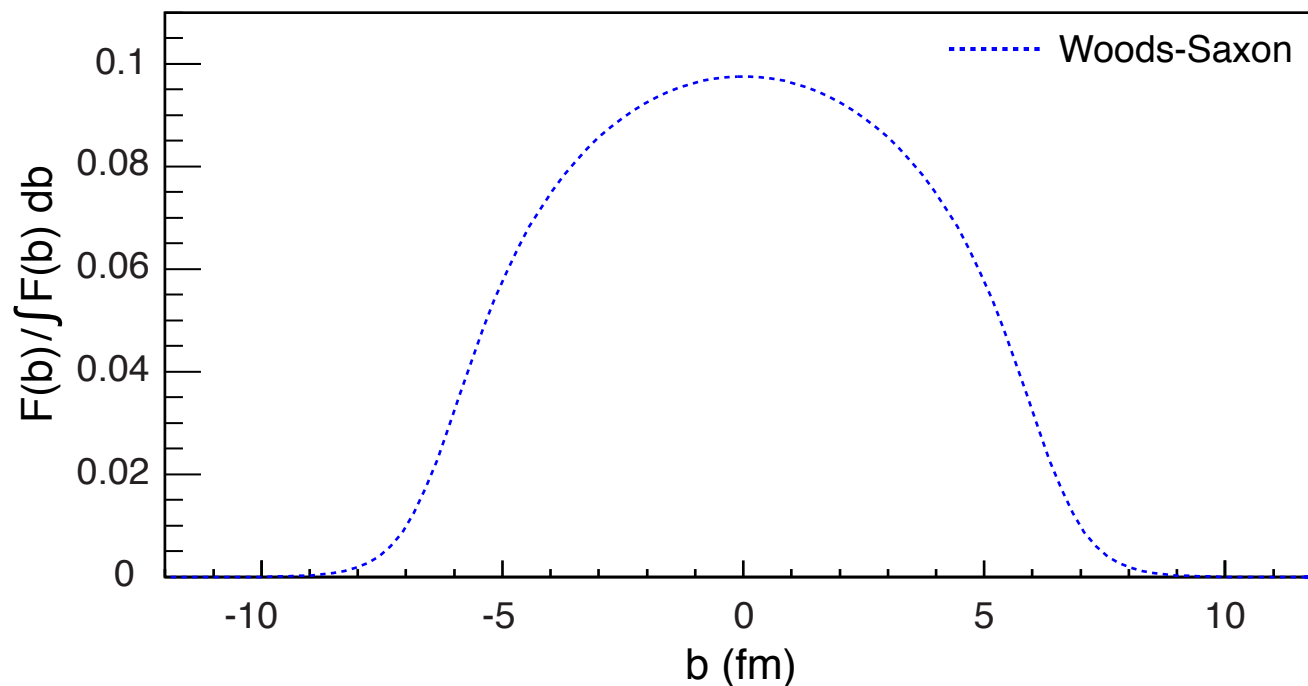
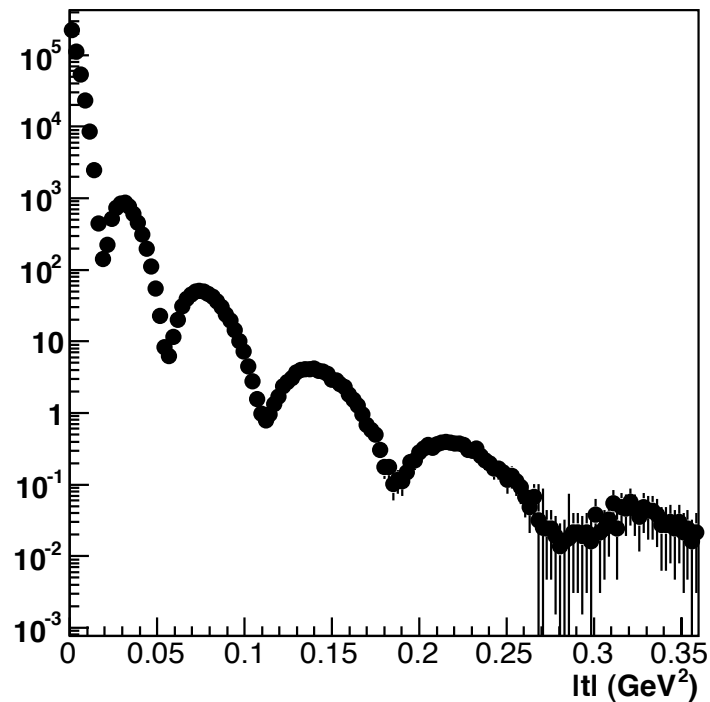


Integration routines have their issues with Bessel functions  
Use GSLIntegration (best available) - makes a difference!

# t-Range

$\phi$  bNonSat:

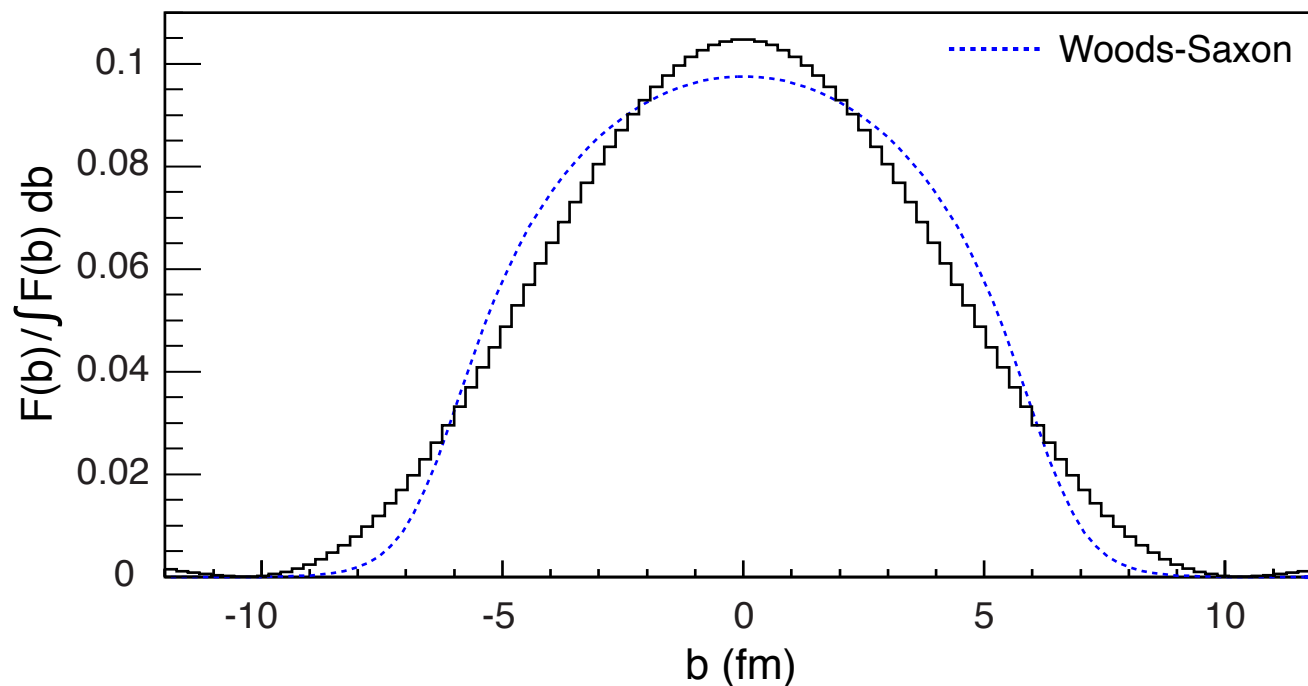
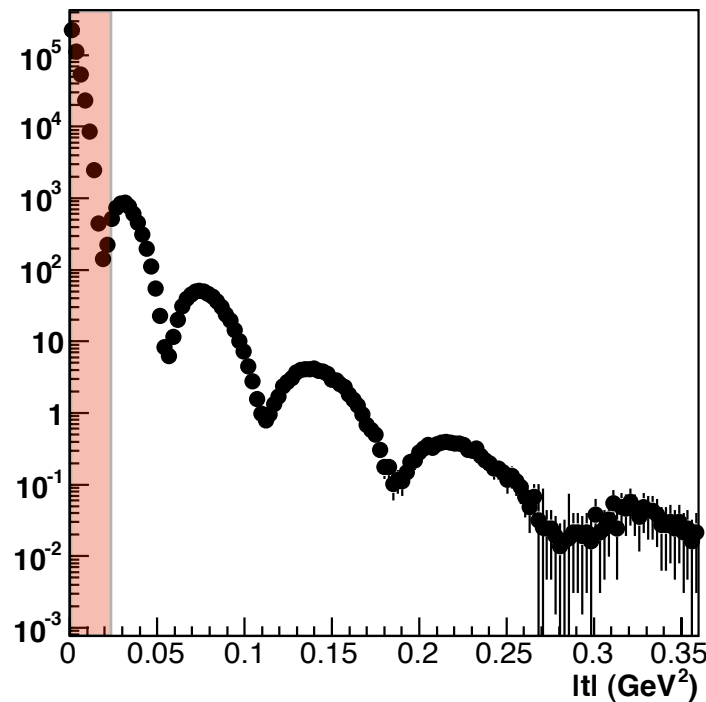
- No saturation effects expected
- In ideal world: should get original Woods-Saxon back



# t-Range

$\phi$  bNonSat:

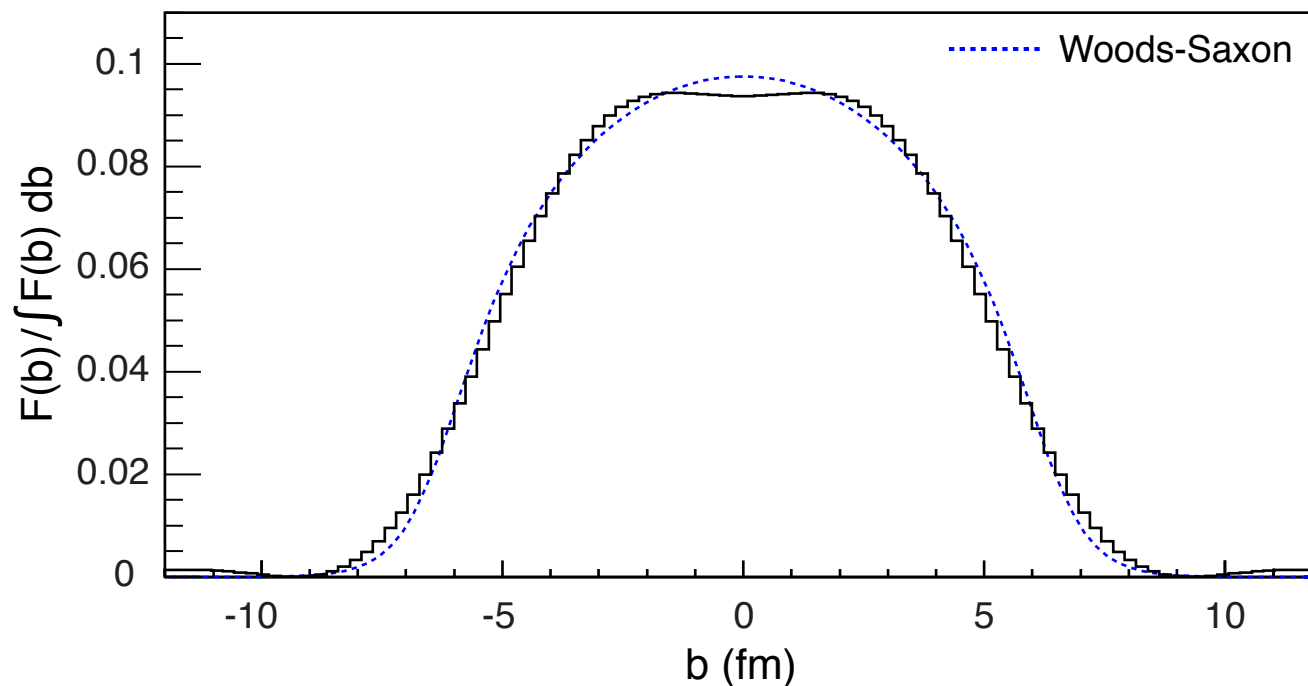
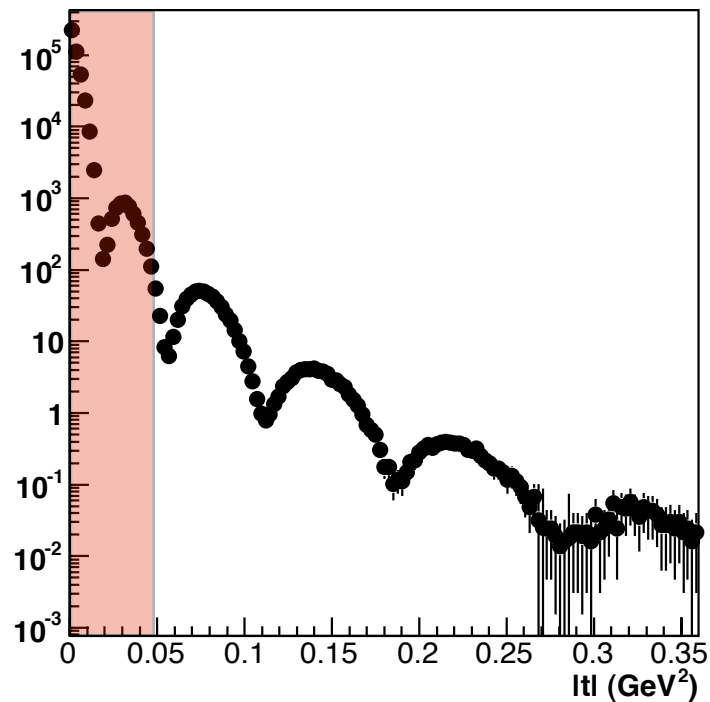
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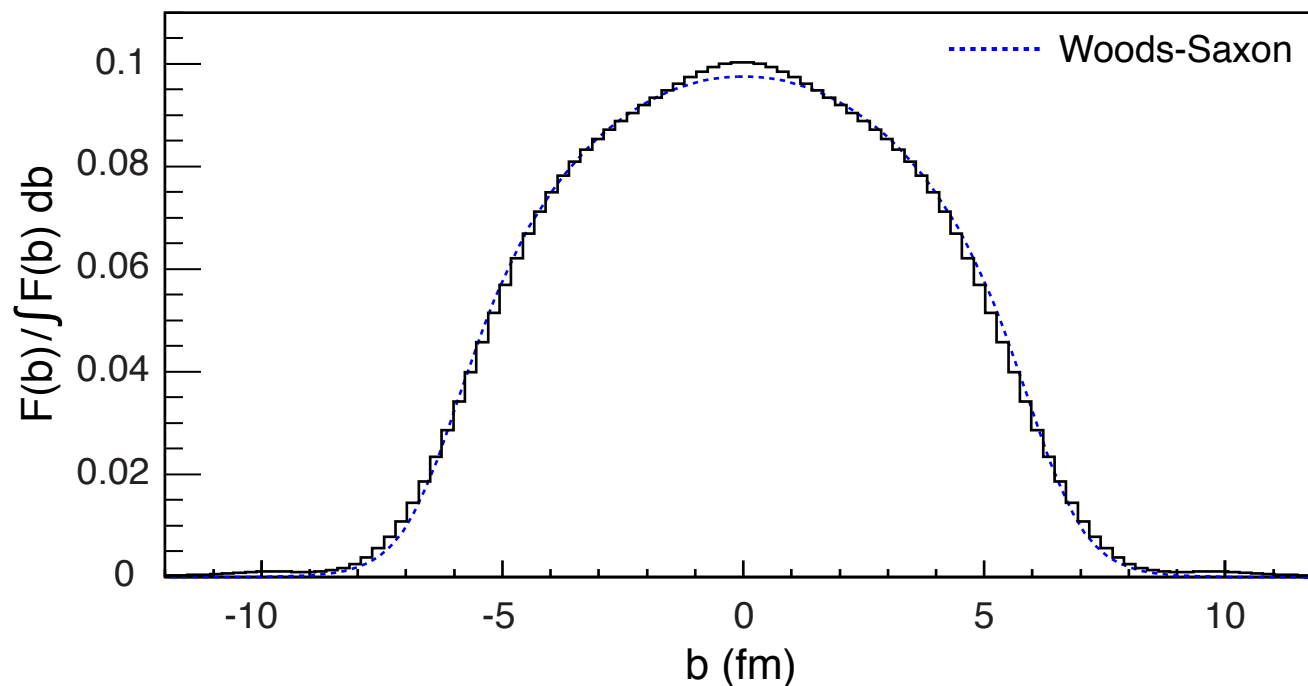
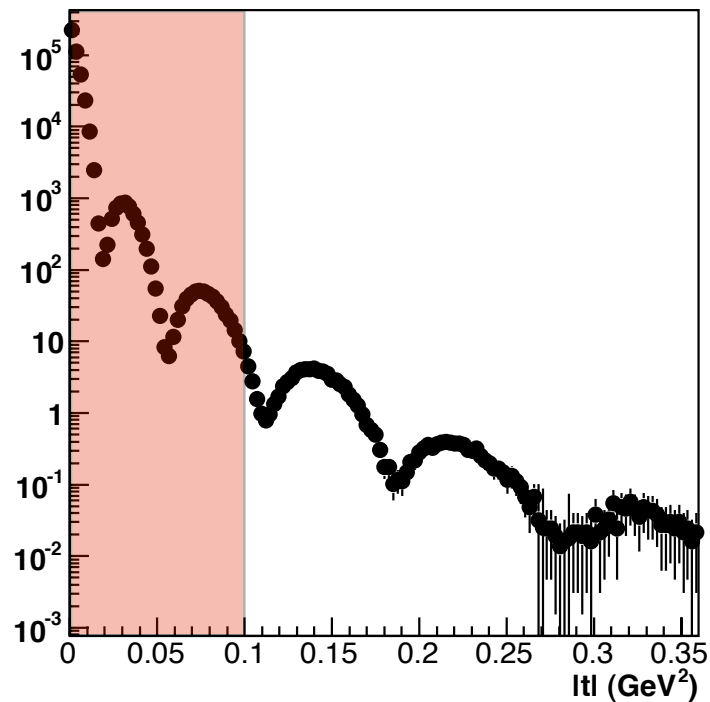




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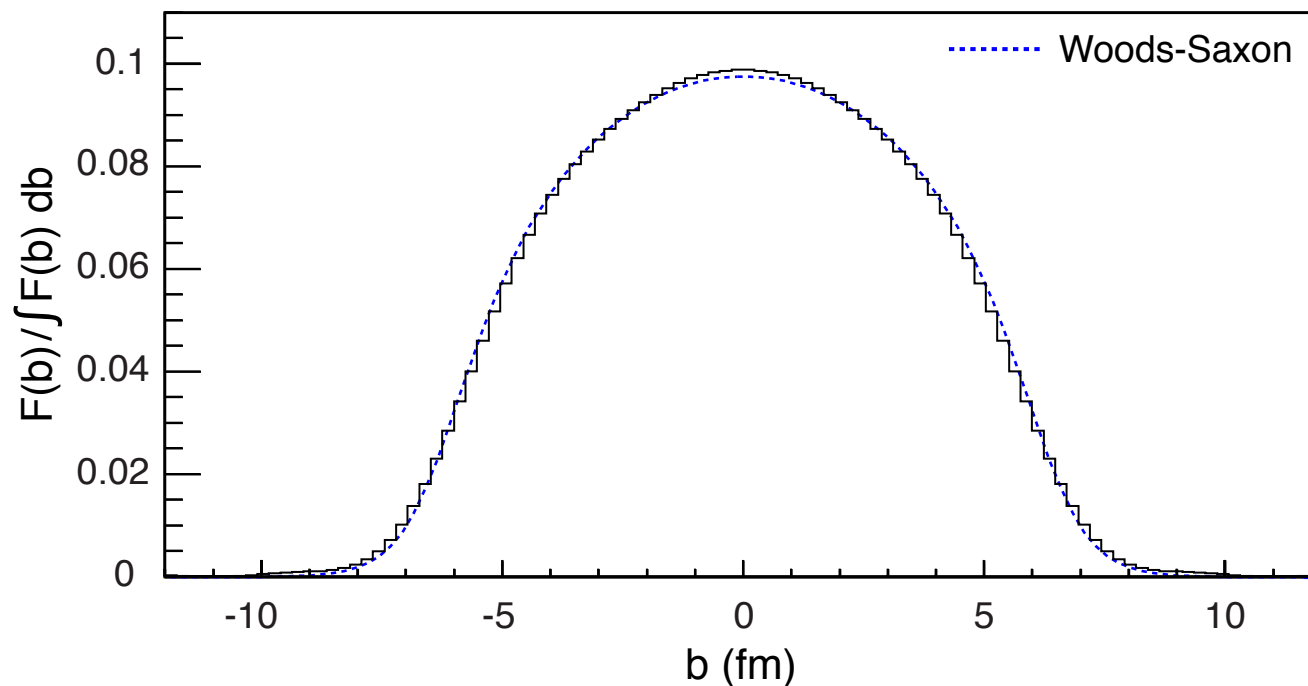
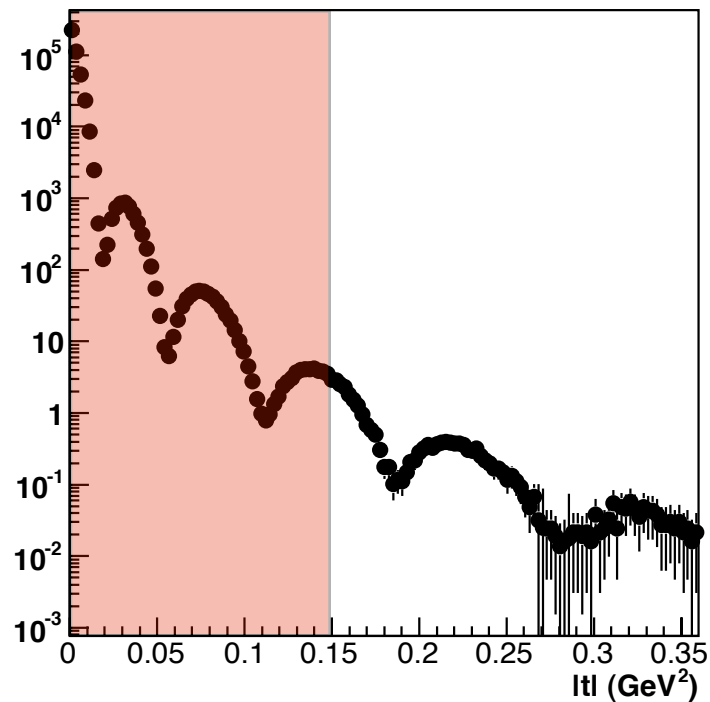
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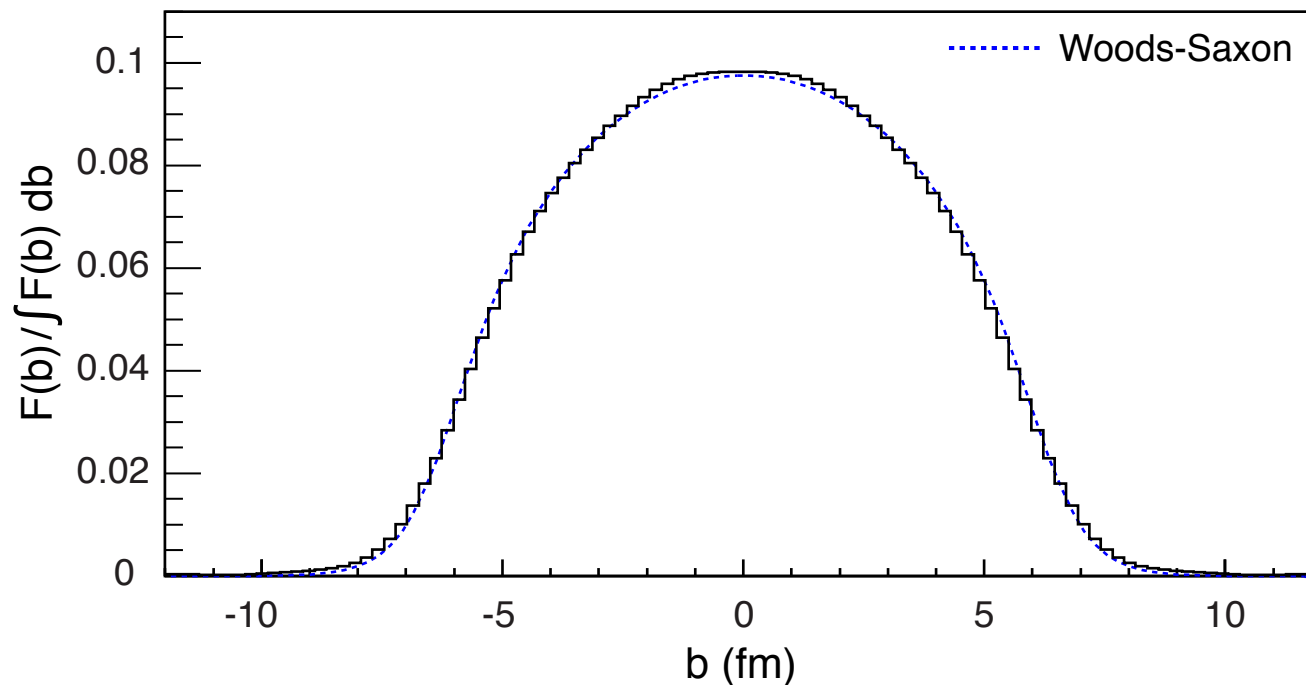
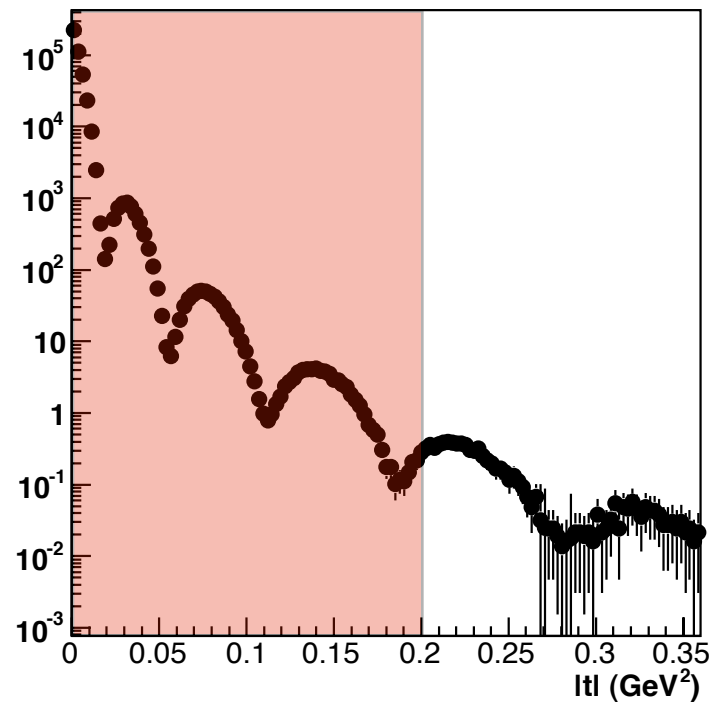
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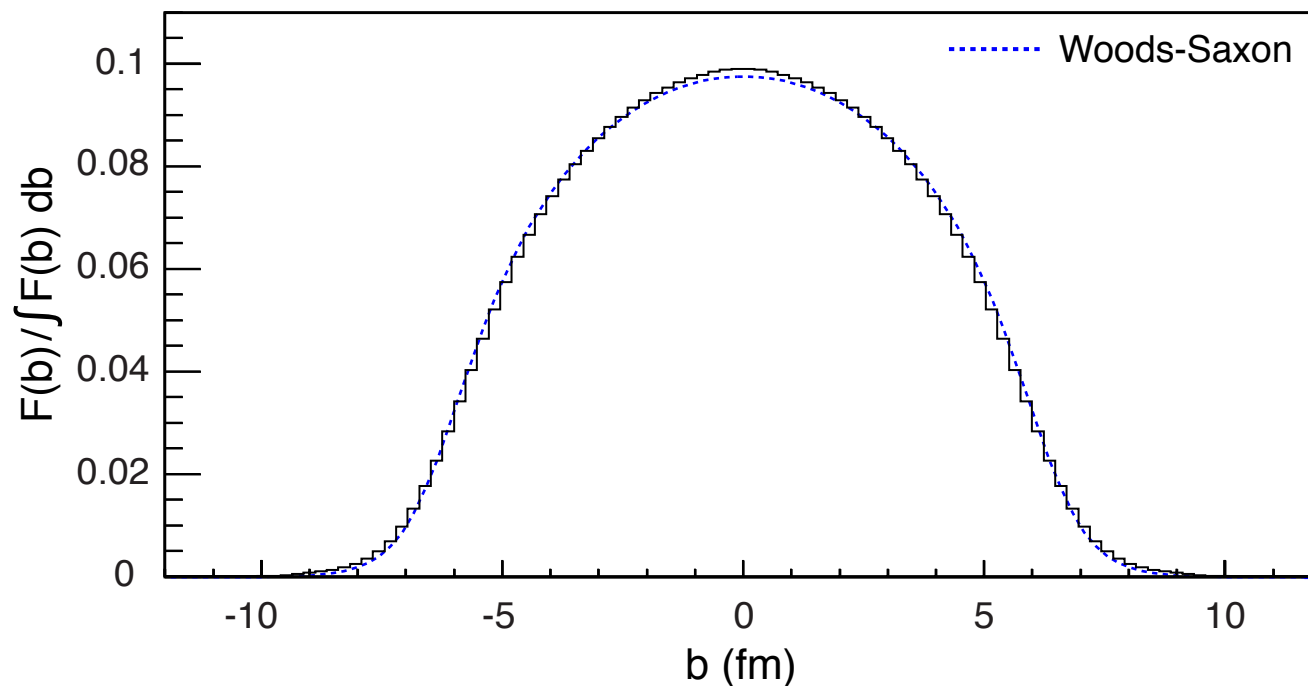
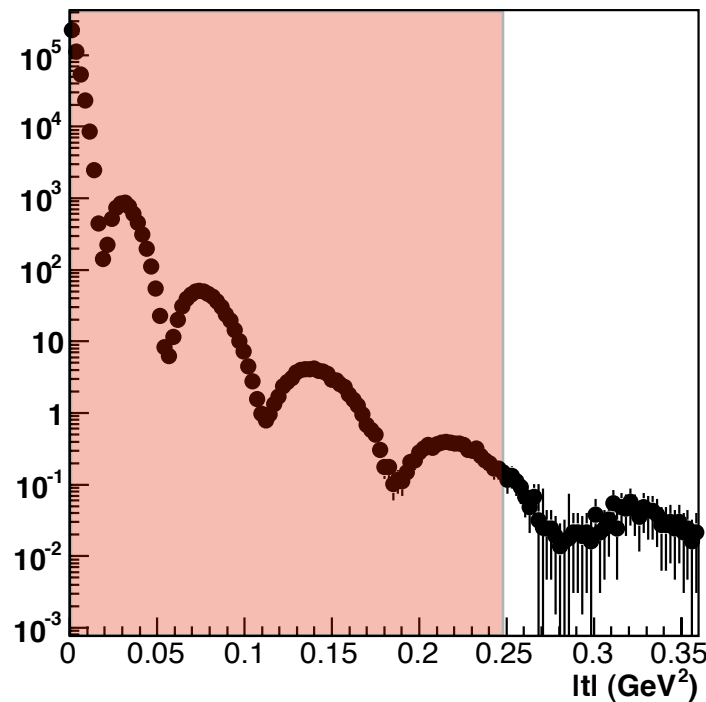
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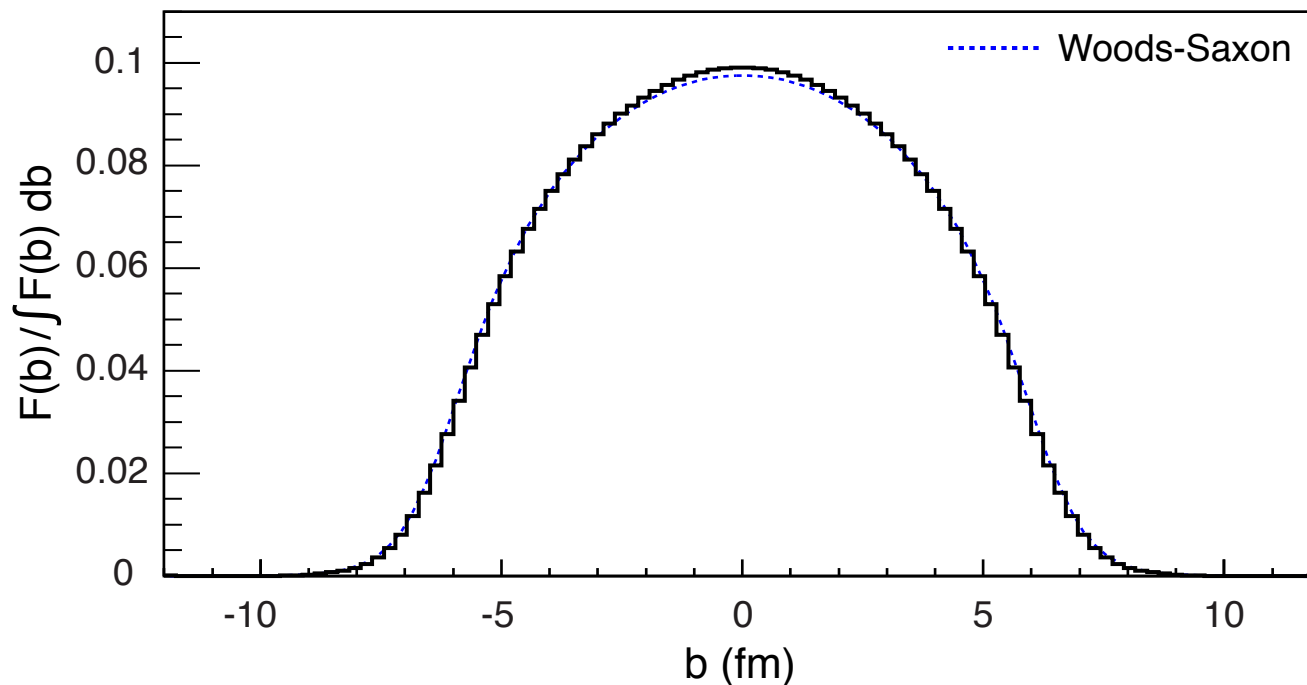
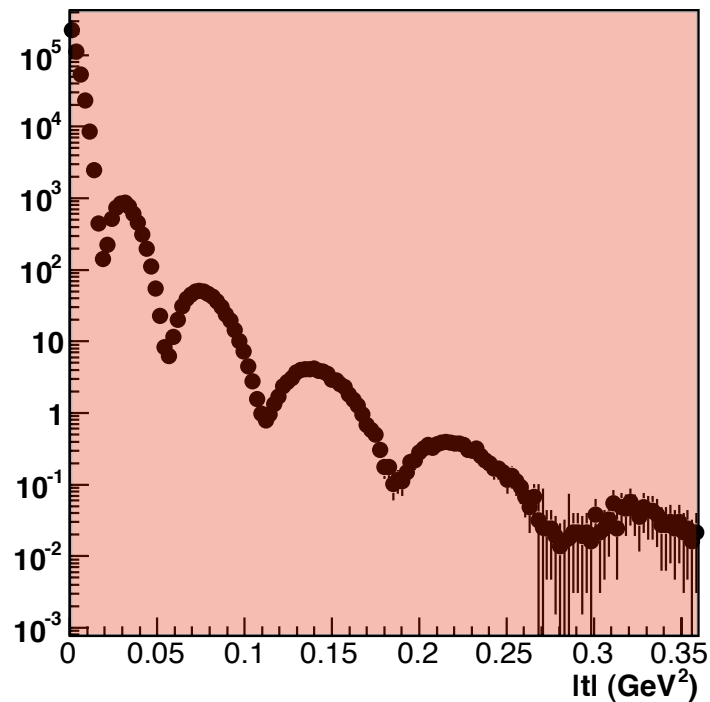
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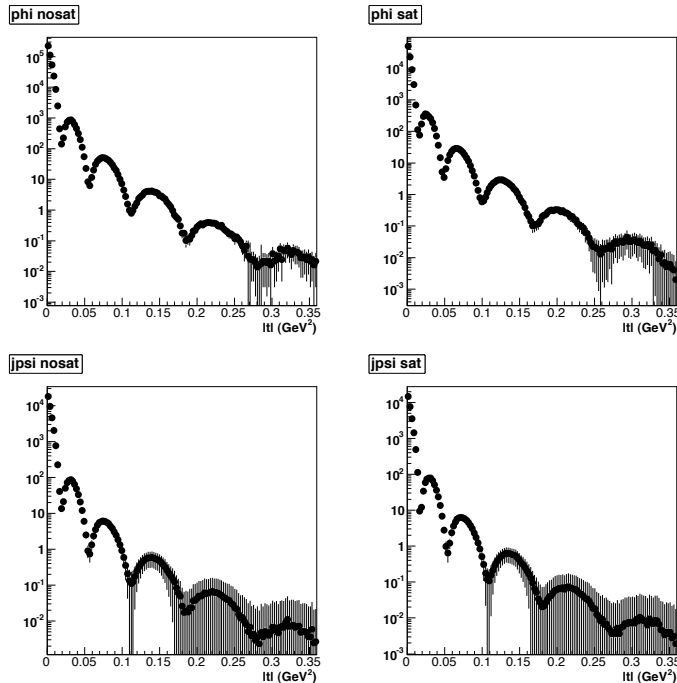
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# Error Band?



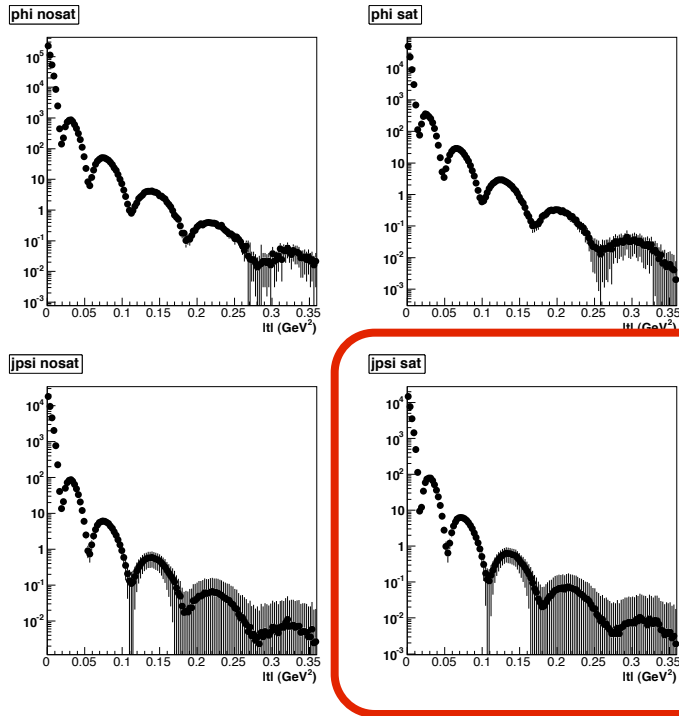
Use 2 extremes:

1.  $d\sigma/dt|_{\text{upper}} = d\sigma/dt + \text{error}(t)$
2.  $d\sigma/dt|_{\text{lower}} = d\sigma/dt - \text{error}(t)$

Run both through same procedure as curve itself. In each bin pick min and max of  $(d\sigma/dt, d\sigma/dt|_{\text{lower}}, d\sigma/dt|_{\text{upper}}) \Rightarrow$  error band



# Error Band?

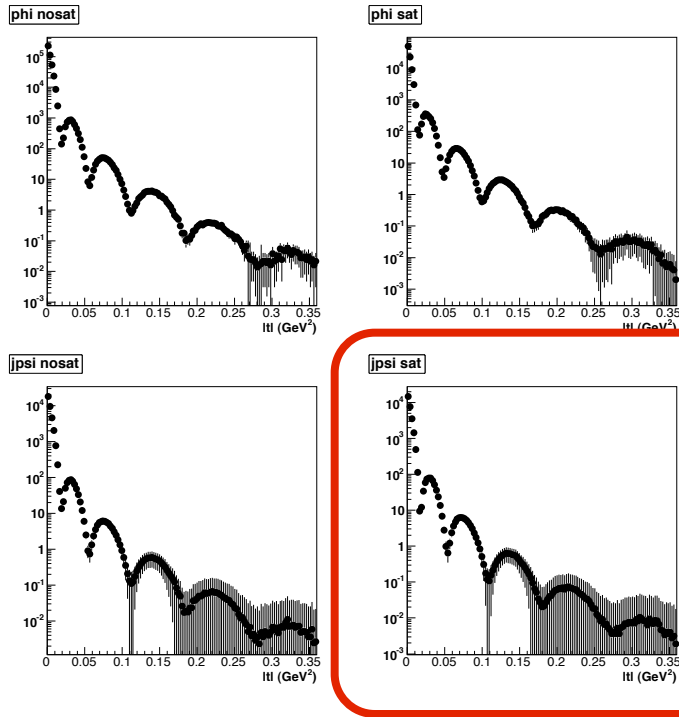


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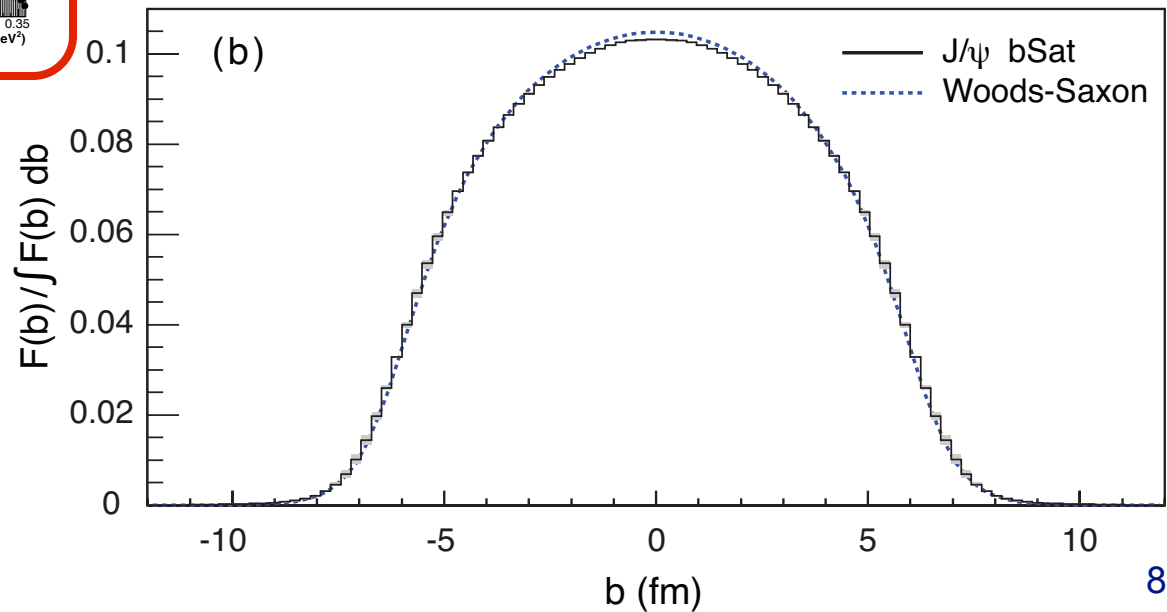
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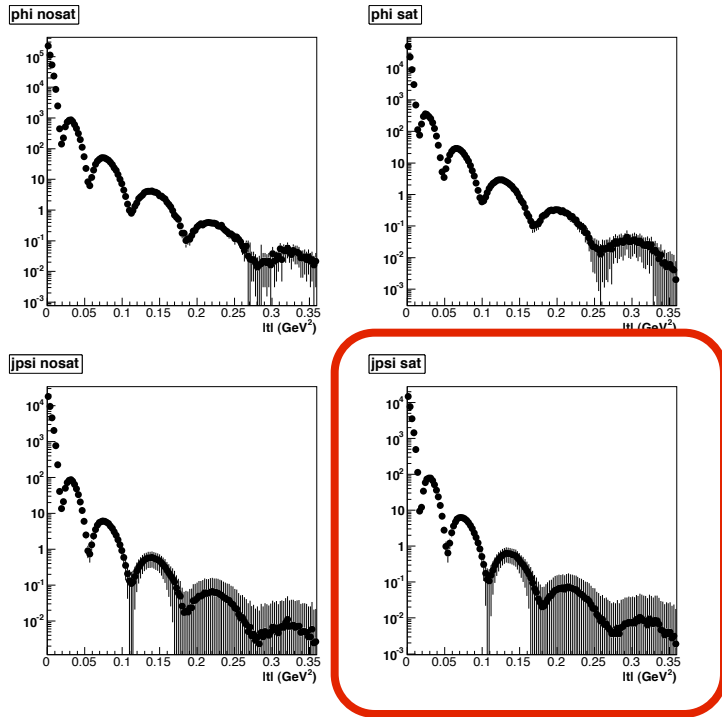
Here  $J/\psi$  sat:

$\Rightarrow$  tiny errors

$\Rightarrow$  almost invisible



# Error Band?



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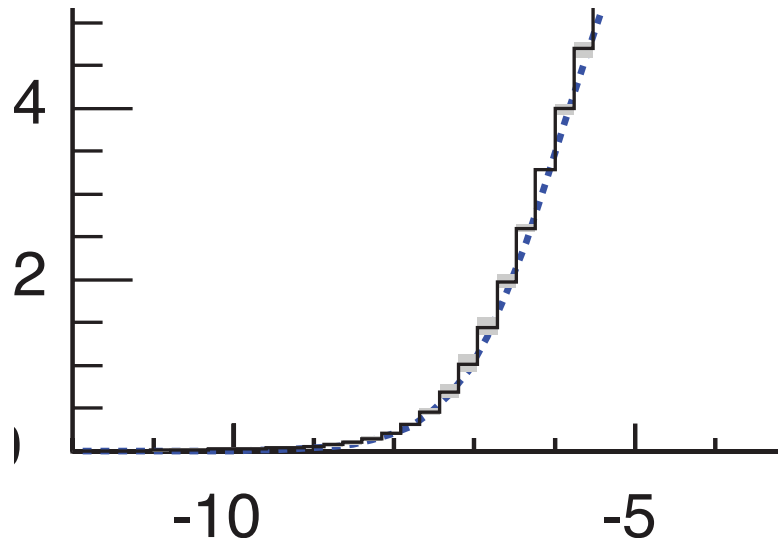
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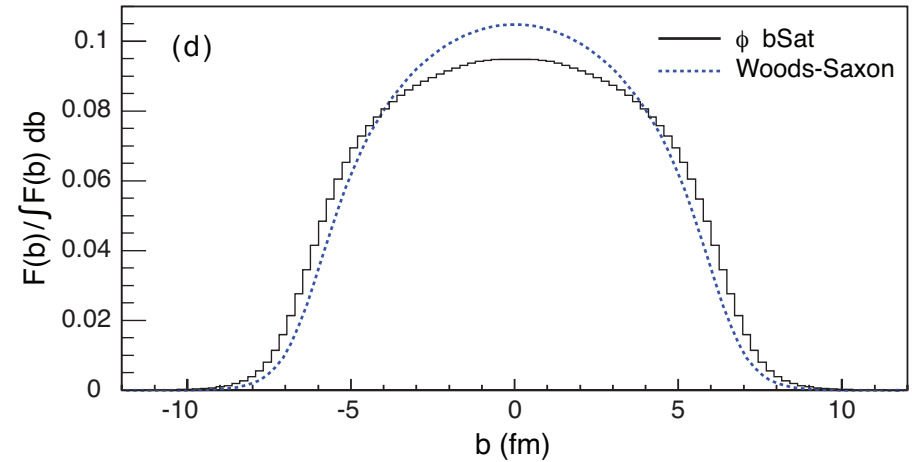
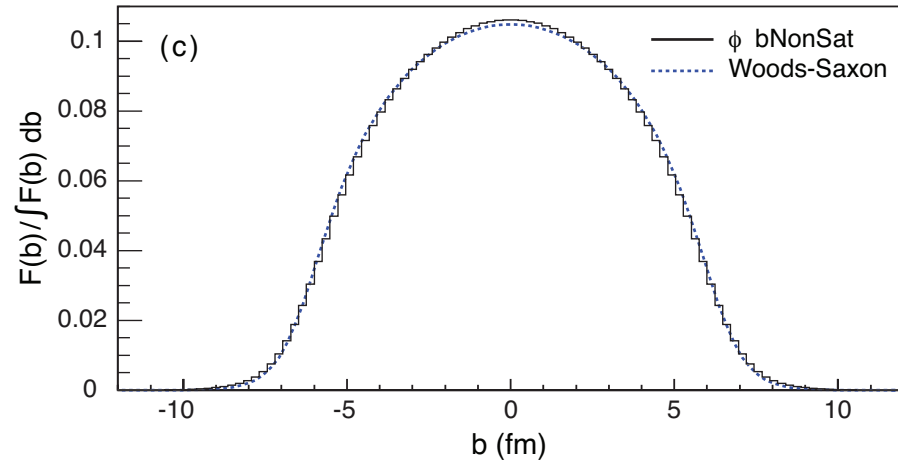
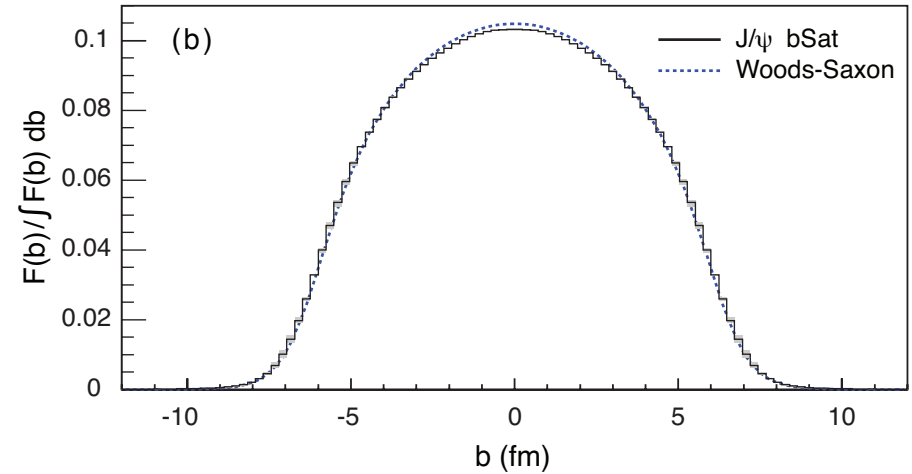
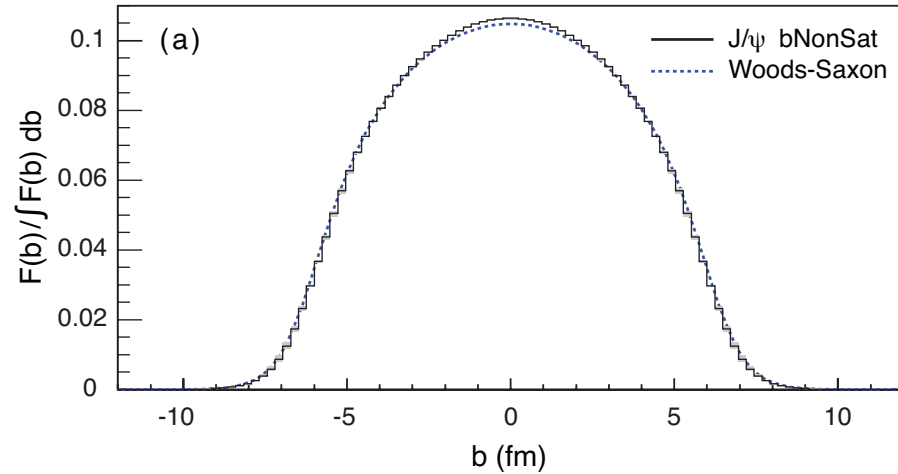
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# Results for all Data Sets



# Summary

---

$d\sigma/dt \rightarrow F(b)$

- works better than expected
- $-t < 0.2 \text{ GeV}^2$  is more than enough
- little sensitivity for errors (at  $10 \text{ fb}^{-1}$ )
- $J/\psi$  appears to be the best probe for  $F(b)$  independent of saturation effects or not
- $\phi$  shows saturation/coherence effects
  - ▶ OK as a signature for saturation
  - ▶ not so good for studying  $F(b)$